

# *Pollution permits, Strategic Trading and Dynamic Technology Adoption*

Luca Taschini  
(LSE)

(with Santiago Moreno-Bromberg - Uni Zurich)



Ritsumeikan University  
Beppu, March 9th, 2012

Transferable Emissions

In a Nutshell

Contributions

Basic Model

Regulator's Aim

Permit price

Strategic Trading

Technology Adoption

Restore Incentives

Self-financing

Conclusions

References

# Regulation through transferable emissions

- ▶ The main idea behind transferable emission permits is **to create a market** for pollution rights.
- ▶ A pollution right simply represents a permit that consists of a unit (pound, ton, etc.) of a specific pollutant.
- ▶ Transferable permits operates on the basis of the following postulates:
  1. It is possible to obtain a **legally sanctioned right** to pollute.
  2. These rights (permits) are **clearly defined**.
  3. The total number of permits and the initial distribution of the total permits among the various polluters are **assigned by government agencies**.
  4. Polluters emitting in excess of their allowances are subject to a **stiff monetary penalty**.
  5. Pollution permits are **freely transferable**. That is, they can be freely traded in the marketplace.

## Transferable Emissions

In a Nutshell

Contributions

Basic Model

Regulator's Aim

Permit price

Strategic Trading

Technology Adoption

Restore Incentives

Self-financing

Conclusions

References

# Adoption of low pollution–emitting technologies

- ▶ A key consideration when **choosing a policy** is the **incentives** it provides to regulated agents to **invest** in new technologies or **adopt** alternative, low pollution–emitting technologies;
- ▶ In most of the cases, the adoption of low pollution–emitting technologies **permanently** reduces future emissions.
- ▶ This has clear consequences on the **future needs of permits** and, more importantly, on the **future incentives** to adopt new technologies.
- ▶ Most of the current literature neglects the impact of **aggregate reductions** on the *allowances supply*.
- ▶ Including this in the analysis would showcase an **individual firm's incentives** to adopt low pollution–emitting technology.

# Positioning in the existing literature

- ▶ Biglaiser et al. [1995] show that under a system of tradable permits, technology adoption is **distorted** because individual regulated companies may have a **significant effect** on the **aggregate supply** of permits.
- ▶ They, however, **assume** that companies are **price-takers**, and do not investigate the impact on the incentives for technology adoption of strategic exchanges of permits.
- ▶ As shown by Kennedy and Laplante [1999], **under imperfect competition** standard results might have to be revised.
- ▶ In this paper we determine the firms' optimal **compliance strategy** (permit trading and timing of the technology adoption) when companies are not price takers.

# The paper in a nutshell

- ▶ This paper examines a pollution–constrained economy, where it is assumed that the **regulator** does **not anticipate** the adoption of new technology.
- ▶ The regulator sets an **optimal** and **credible** policy by committing to the **type** of policy instrument and its **level**,  $\{N(t), P\}$ , for a sufficiently long period of time,  $T$ .
- ▶ Regulated firms can determine their **compliance strategies** by choosing between investment in low pollution–emitting technologies and trading emission permits.
- ▶ The firms' emissions are **technology-specific** and are subject to **economic shocks**.
- ▶ The adoption of new technologies is assumed to **affect** only the amount of **pollution** emitted for given output or input, and does not otherwise affect production.

# Approach and contributions of the paper

We use a game-theoretical approach to model the formation of permit prices and investigate how the policy levels affect the incentive to adopt new technology under a transferable permits system.

The contribution of the paper is threefold:

1. To investigate the **strategic trading behavior** of market participants that underpins the allowance price formation.
2. To study the **incentive to adopt** low pollution-emitting technologies in a **dynamic** setup.
3. To propose and implement a criterion for the selection of a *self-financing* policy that **restores the dynamic incentives** to invest in low pollution-emitting technologies.

# The subjects in the model

- ▶ A group of (risk averse) firms ( $\mathbb{I} = 1, \dots, m$ ), which operate in a pollution–constrained economy under a transferable permits system.
  - ▶ Firms are **not** price takers on the permit market.
  - ▶ Firms can **adopt** low pollution–emitting production **technologies** and **exchange permits**.
  - ▶ Firms are characterized by their **stochastic emission profiles**, as well as by the costs of abatement **investments**.
- ▶ A regulator whose intention is to control pollution and promote the adoption of low pollution–emitting technologies.
  - ▶ The regulator identifies an **optimal** and **credible** emission reduction **target**, the overall **length** of the commitment **period** and the **enforcement structure**.
  - ▶ The regulator (cannot) does **not anticipate** the adoption of new technologies.





# Firms characterization: pollution emissions

- ▶ We denote the cumulative emissions of firm  $i$  up to time  $t$  by  $Q(t)$ , which is modeled by

$$Q_h^i(t+1) = \begin{cases} u_h^i(t) \cdot Q^i(t), & \text{with probability } q(t). \\ d_h^i(t) \cdot Q^i(t), & \text{with probability } 1 - q(t), \end{cases}$$

Here  $h \in \{o, n\}$  denotes whether or not the firm is operating under the **old** or **new** technology,  $u_h^i(t) > d_h^i(t) > 1$ , and  $u_o^i(t) > u_n^i(t)$  and  $d_o^i(t) > d_n^i(t)$  (more below).

- ▶ The firms' emissions are subject to **economic shocks** and their current **technology status  $h$** .
- ▶ Demand for a firm's products is contingent on phenomena that are beyond its grasp (a widespread crisis, for example). Therefore,  $u_h^i(t)$  and  $d_h^i(t)$  are **exogenous** and represent the (uncontrollable) state of the economy.

# Adoption of new technology

Each firm has the alternative to adopt low pollution–emissions technology. In particular, we assume:

- ▶ Decisions to adopt technology over the period  $[t, t + 1]$  are made at time  $t$ , and they come into effect **instantaneously**.
- ▶ The investment in the new technology occurs only once during the phase, and it is **non–reversible**.
- ▶ Adoption of the new technology affects only the amount of pollution emitted for given output or input, and **does not** otherwise **affect production**.
- ▶ Firm  $i$  must **spend**  $C^i$  if it wishes to change its pollution emission profile.
- ▶ The future value of the investment is computed using an interest rate  $r > 0$ , which we assume remains **constant** throughout the phase.

# Realized net pollution emissions

Emissions are **verified** at the end of each period. Compliance requires firms to **completely offset** their emissions either using allocated permits or purchasing permits on the exchange.

- ▶  $\Delta Q_{\zeta,h}^i(t+1)$  denotes the pollution emissions over  $[t, t+1]$  under the economy state  $\zeta$  and technology  $h$  for firm  $i$ -th.
- ▶ The realization of the  $\Delta Q_{\zeta,h}^i(t+1) - N^i(t)$ 's determines the firms' positions in the permits market.
  - ▶ If  $\Delta Q_{\zeta,h}^i(t+1) - N^i(t) > 0$  than the firm *must purchase* permits in the market or **pay the penalty  $P$** .
  - ▶ If  $\Delta Q_{\zeta,h}^i(t+1) - N^i(t) < 0$  than the firm *can offer* the permits in the exchange **for a profit**.
- ▶ Trading takes place at the end of each period.

# Realized vs. expected net pollution emissions

- ▶  $\Delta Q_{\zeta}^i(t+1) - N^i(t)$ 's determines the **realized** firms' positions in the permits market.
- ▶  $x_i(t+1, h) := \mathbb{E}[\Delta Q^i(t+1, h) - N^i(t)]$  represents firms' **expected** emissions. These quantities are used to make decisions regarding investments in the new technology, given technology status  $h$ .
- ▶ Let  $s(t+1, h)$  and  $d(t+1, h)$  be the **supply** and **demand** sides of the market (in terms of the firms expected positions), respectively.
- ▶ Then,

$$S(t+1, h) := - \sum_{i \in S} x^i(t+1, h) \text{ and } D(t+1, h) := \sum_{i \in D} x^i(t+1, h)$$

represents the (expected) number of unused permits, i.e. the **aggregate supply**, and the (expected) number of nonoffset emissions, i.e. the **aggregate demand**.

# The regulator's objective - cap emissions

Before proceeding with the analysis of the generation of prices and the technology adoption, we stress that the following policy levels have been optimally chosen at time  $t = 0$ :

1. The **allocation of allowances**  $\{N^i(t)\}$ , i.e.  $\alpha_i(t), \beta_i(t)$ ;
2. The **penalty** level  $P$ .
3. The **length** of the phase  $T$ ;

The regulator's aim is to spur technology adoption by **controlling emission** via emission permits. We observe how these policy levels interact with the **incentive** for technology adoption through time.

# Generation of allowance prices

- Prices are generated by “supply-and-demand”. We define the **supply-demand ratio**

$$\mathcal{R}(t+1, h) := -\frac{S(t+1, h)}{D(t+1, h)},$$

and, consistent with Seifert et al. [2008], Chesney and Taschini [2011], and Carmona et al. [2009] we define the permit price  $\Pi$

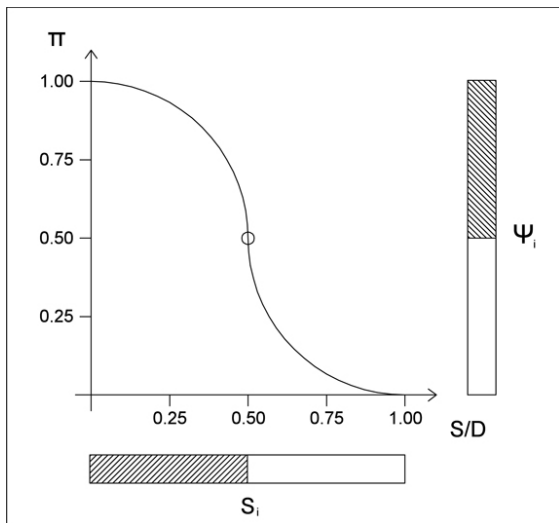
$$\Pi(t+1, h) := P \cdot \eta_{\mathcal{R}(t+1, h)} \left( -\frac{S(t+1, h)}{D(t+1, h)} \right)$$

where  $P$  is the penalty level and  $\eta_{\mathcal{R}}$  is a (reaction) function  $\eta_a : [0, a] \rightarrow [0, 1]$

$$\eta_a(x) := \begin{cases} \exp \left\{ \frac{x^2}{x^2 - a^2} \right\}, & \text{if } x \in [0, a), \\ 0, & \text{otherwise.} \end{cases}$$

- By construction  $0 \leq \Pi(t+1, h) \leq P$ .

# Graphical representation of allowance prices



Transferable Emissions

In a Nutshell

Contributions

Basic Model

Regulator's Aim

**Permit price**

Strategic Trading

Technology Adoption

Restore Incentives

Self-financing

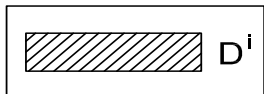
Conclusions

References

# Aggregate demand and supply

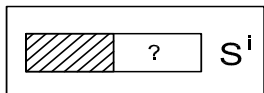
## Aggregate demand

Firms in shortage of permits face severe penalties if they fail to deliver an amount of allowances equal to their emissions. So it is in the buyers' ( $d$ ) best interest to offset all their emissions at **any price** lower than the penalty level  $P$ .



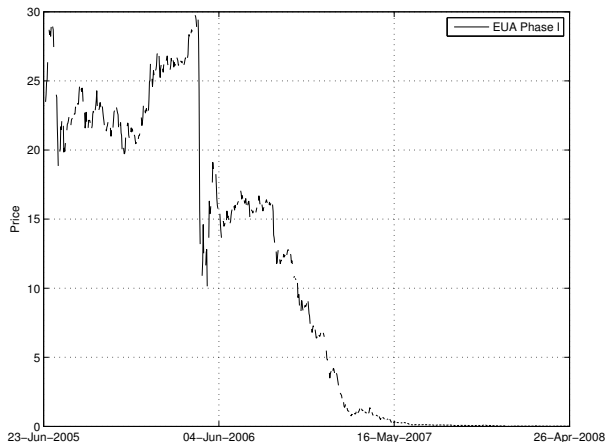
## Aggregate supply

On the other hand, the lower the aggregate supply,  $S$ , the higher the exchange value,  $\Pi$ . Therefore, it may very well be in the sellers' best interest to **reduce** the availability of permits and **increase** the allowance exchange value. In fact, there is a **trade-off** between offering a higher number of cheap permits, or less of them, but at a higher value.





# Example: the first phase of the EU ETS



**Figure:** Spot price of the EU Allowance Unit from 2005 until 2008 on the European Climate Exchange (ECX).

# Theorem: Non-cooperative game

Let  $-i$  represent all firms except  $i$ , and let firm  $i$ 's payoff be

$$\Psi^i(x^i, x^{-i}) = x^i P \cdot \eta_{\mathcal{R}} \left( - \frac{S^{-i} + x^i}{\mathcal{D}} \right),$$

We construct an  $m_s := \#s(t+1, h)$  (non-cooperative) game and show it possesses a **unique** pure-strategy Nash Equilibrium.

We show that the *expected equilibrium exchange value* of an allowance, contingent on  $h$  is:

$$*\Pi(t+1, h) = P \cdot \eta_{\mathcal{R}(t+1, h)} \left( - \frac{*S(t+1, h)}{\mathcal{D}(t+1, h)} \right)$$

where  $*S(t+1, h) = \sum_{i \in m_s} *x^i(t+1, h)$ , and  $*x^i(t+1, h)$  are the best responses.

# Firms' investment decision

- ▶ Technology adoption is determined **endogenously** and it depends on the **(uncertain) future supply** and **demand** of permits.
- ▶ The incentives for a firm in permit excess hinge on the firm's **potential profits**, i.e. on the ability to sell unused permits for a high price.
- ▶ The incentives for a firm in the need for permits depend on the firm's **potentially avoided penalty costs**, i.e. on its ability to reduce emissions by the use of new technologies.
- ▶ To quantify these amounts, each firm computes its corresponding expected payoff for the remainder of the regulated phase, which shall be denoted by  $[t_0, T]$ , over all **possible technology scenarios**.
- ▶ A family of firm-specific and concave utility functions,  $\Upsilon^i$ , is used to assess if the adoption of new technology at time  $t$  is **economically viable or not**.

# The technology matrix

- ▶ We define

$$\mathcal{O}(t_0) := \{i \in \mathbb{I} \mid \mu^i(t_0 - 1) = \mu_o^i(t_0 - 1)\}.$$

which represents the set of firms that have not changed technology up to time  $t_0 - 1$ ;

- ▶ We consider the set  $\mathcal{M}(t_0)$  of matrices of dimension  $\#\mathcal{O}(t_0) \times (T - t_0)$ , where each row contains a single 1 and the rest of its entries are 0's.

This firm adopts at time  $t = t_0 \longrightarrow$

$$\begin{pmatrix} 0 & 1 & 0 & \cdots & 0 \\ 1 & 0 & \cdots & \cdots & 0 \\ 0 & 0 & 0 & \cdots & 1 \end{pmatrix}$$

# Technology matrix and associated payoffs

- ▶ We distinguish between firms that adopt the new technology

$$\mathcal{M}_n^i(t_0) := \{M \in \mathcal{M}(t_0) \mid M(i, 0) = 1\},$$

and firms that decide to wait at time  $t_0$

$$\mathcal{M}_o^i(t_0) := \{M \in \mathcal{M}(t_0) \mid M(i, 0) = 0\}.$$

- ▶ For  $k \in \{o, n\}$ , we define the **payoffs vector** associated to  $\mathcal{M}_k^i(t_0)$  as

$$\Upsilon^i(t_0, k) := (1/\#\mathcal{M}_k^i(t_0)) \sum_{j=1}^{\#\mathcal{M}_k^i(t_0)} U^i(\mathcal{V}_k^j(t_0)).$$

where  $\mathcal{V}_k^j(t_0)$  represents the future profits under technology  $k$ .  
**If**  $\Upsilon^i(t_0, n) \geq \Upsilon^i(t_0, o)$ , then firm  $i$  **adopts** the low-emitting technology at time  $t_0$ , **otherwise it waits**.



# Restore the incentive to adopt new technology

**Proposition** Under identical primitives and identical triples  $(T, \{N^i(t)\}_{i \in \mathbb{I}}, P)$ , the following holds for all  $t \in [0, T]$  :

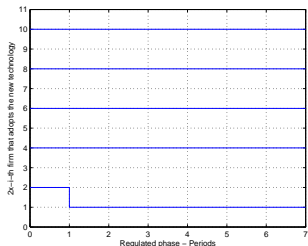
$${}^4\Pi^*(t+1, h) \geq \Pi^*(t+1, h).$$

**Remark** By construction, if  $i \in s(t+1, h)$ , for any  $h$  we have that

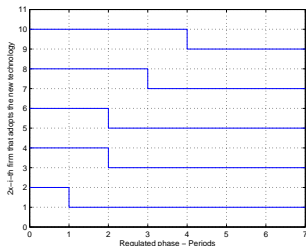
$${}^4\phi^i(t+1, h) \geq \phi^i(t+1, h).$$

From previous Proposition, if  $i \in d(t+1, h)$  then

$${}^4\phi^i(t+1, h) \leq \phi^i(t+1, h).$$

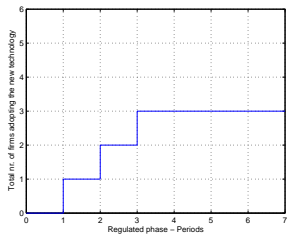


(a) Firm-wise technological adoption without EC4P

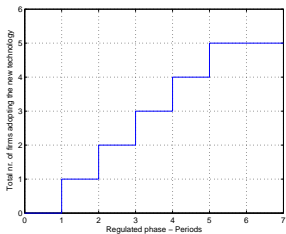


(b) Firm-wise technological adoption with EC4P

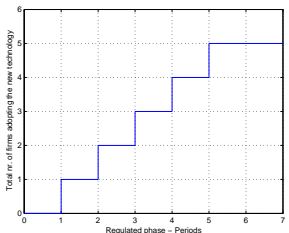
# Controlling also the timing of the adoption



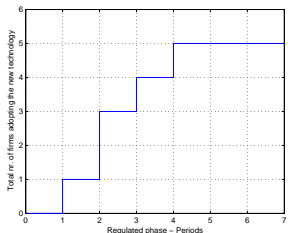
(c) Aggregate technology adoption for  $P_g = 1.5$



(d) Aggregate technology adoption for  $P_g = 2.5$



(e) Aggregate technology adoption for  $P_g = 3.5$



(f) Aggregate technology adoption for  $P_g = 4.5$



# Risk assessment of the cost of the policy

- ▶ The purpose of introducing this instrument is to have a contingent policy that allows to “control” permits supply and continue to **promote technology adoption**.
- ▶ This, however, comes **at the expense** of the payments to be made to firms that exercise their contracts.
- ▶ Yet, the regulator **collects funds** from the firms that make **penalty** payments, which may be used to (partially) cover the EC4Ps.
- ▶ We present a methodology to **assess the likelihood** that the collection of such payments renders the policy budget compatible, so-called “*self-financing*”, i.e. that tax-payers’ funds are **not required** to cover the cost of its implementation.

# Risk assessment of the cost of the policy

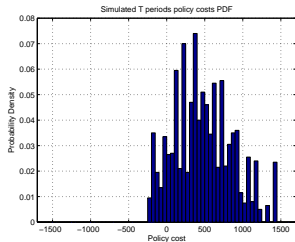
- ▶ Let  $X_I$  denote potential incomes, penalty payments, and let  $X_O$  denote potential outcomes, EC4Ps.
- ▶ We use value-at-risk to perform an analysis of **how plausible** it is that a policy turns out to be self-financing.
- ▶ For a given  $\rho$ , the assessment  $\rho(X_I - X_O)$  provides a **measurement** of whether or not the permits system endowed with EC4Ps is self-financing.
- ▶ For fixed  $\{T, \{N(t)\}\}$ , the parameters  $P$  and  $P_g$  **completely determine**  $\rho(X_I - X_O) =: f(P, P_g)$ .
- ▶ This risk assessment is based on the previous examples and it is evaluated by performing Monte Carlo simulations of pollution emissions used to **approximate the PDFs** of  $(X_I - X_O)$ .

# Value-at-risk of the contingent policy

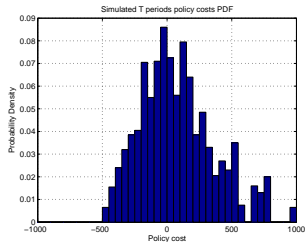
$V@R_{\rho}(X_I - X_O)$				
$P_g$				
$\rho$	1.5	2.5	3.5	4.5
0.10	-30.8	-274.6	-397.0	-704.5
0.05	-123.5	-344.6	-476.3	-798.1
0.01	-187.5	-424.9	-594.9	-944.7

Table:  $V@R_{\rho}(X_I - X_O)$  for standard confidence levels  
 $\rho = \{0.10; 0.05; 0.01\}$ .

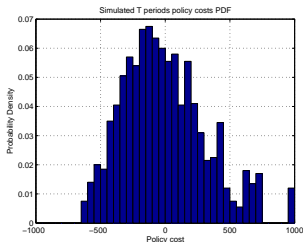
# Numerical evaluation of the PDFs of $X_I - X_0$



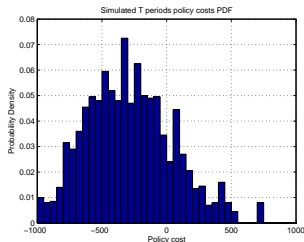
(a) PDF for  $P_\sigma = 1.5$



(b) PDF for  $P_\sigma = 2.5$



(c) PDF for  $P_g = 3.5$



(d) PDF for  $P_g = 4.5$

Figure: Probability density functions for different levels of  $P_g$ ,  $P = 10$ .

# Conclusions

In this paper:

1. Technology adoption and allowance price are generated **endogenously** and are inter-dependent.
2. It is shown that the non-cooperative permit trading game possesses a **pure-strategy** Nash equilibrium, where the allowance value **reflects** the level of **uncovered pollution** (demand), the level of **unused allowances** (supply), and the **technological status**.
3. These conditions are also satisfied when a **price support instrument**, which is contingent on the adoption of the new technology, is introduced.
4. Numerical investigation confirms that this policy generates a **floating price floor** for the allowances, and it maintains the dynamic incentive to invest.
5. Given that this policy comes at a cost, a **criterion for the selection** of a “*self-financing*” policy is proposed and implemented.

# Disclaimer

**Disclaimer** Our main aim is to study the influence of the regulator's decisions on the **dynamic evolution** of the technological vector. On this same token, the introduction of a criterion to measure the likelihood of the policy being self-financing is **not** done in the spirit of **minimizing social costs**. In the numerical implementations, we compare the effect of different levels of  $P$  and  $P_g$  on the distribution of  $X_I - X_O$  (and therefore on  $\rho$ ), and simultaneously on the adoption of low pollution-emitting technologies. It might be the case that a choice of primitives that yields very rapid technology adoption of all firms is too socially costly. The analysis of such scenario is not undertaken in this paper.

Transferable Emissions

In a Nutshell

Contributions

Basic Model

Regulator's Aim

Permit price

Strategic Trading

Technology Adoption

Restore Incentives

Self-financing

Conclusions

References

# References I

- G. Biglaiser, J. K. Horowitz, and J. Quiggin. Dynamic Pollution Regulation. *Journal of Regulatory Economics*, 8:33–44, 1995.
- R. Carmona, M. Fehr, J. Hinz, and A. Porchet. Market design for emission trading schemes. *SIAM Review*, 9(3):465–469, 2009.
- M. Chesney and L. Taschini. The Endogenous Price Dynamics of the Emission Allowances and an Application to CO<sub>2</sub> Option Pricing. *Applied Mathematical Finance* - forthcoming, 2011.
- P. Kennedy and B. Laplante. Environmental Policy and Time Consistency: Emissions Taxes and Emissions Trading. In E. Petrakis, E. Sartzetakis, and A. Xepapadeas, editors, *Environmental Regulation and Market Power*. Edward Elgar Publisher, Cheltenham, U.K., 1999.
- J. J. Laffont and J. Tirole. A Note on Environmental Innovation. *Journal of Public Economics*, 62:127–140, 1996.
- J. Seifert, M. Uhrig-Homburg, and M. Wagner. Dynamic behavior of CO<sub>2</sub> spot prices. *Journal of Environmental Economics and Managements*, 56:180–194, 2008.